

Bayesian analysis of Latent Infection with non-informative priors

The GENMOD Procedure

Bayesian Analysis

Model Information	
Data Set	WORK.ONFIT
Burn-In Size	2000
MC Sample Size	10000
Thinning	1
Sampling Algorithm	Gamerman
Distribution	Binomial
Link Function	Logit
Response Variable (Events)	ONFIT
Response Variable (Trials)	N

Number of Observations Read	15
Number of Observations Used	15
Number of Events	141
Number of Trials	1500

Response Profile		
Ordered Value	Binary Outcome	Total Frequency
1	Event	141
2	Nonevent	1359

Algorithm converged.

Analysis Of Maximum Likelihood Parameter Estimates					
Parameter	DF	Estimate	Standard Error	Wald 95% Confidence Limits	
Intercept	1	-2.2033	0.1547	-2.5065	-1.9001
CDD	1	0.1071	0.0628	-0.0160	0.2302
RAIN	1	-0.4264	0.1881	-0.7950	-0.0577
WW	1	-0.0060	0.0628	-0.1292	0.1171
Scale	0	1.0000	0.0000	1.0000	1.0000

All the basic information on the Bayesian model is here. It is always advisable the user to check this part before looking at the rest of the output.

As a first step MLE (frequentist) methods are used to generate the parameter estimates. Then Bayesian methods will be implemented.

➤ scale parameter was held fixed.

The MCMC sampling starts with parameters based on (related to) the MLE (frequentist) fit to the data. To get exact same numerical results each time, put in a seed value.

Initial Values of the Chain					
Chain	Seed	Intercept	CDD	RAIN	WW
1	27500	-2.20328	0.107092	-0.42636	-0.00604

Fit Statistics	
DIC (smaller is better)	293.078
pD (effective number of parameters)	4.012

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Posterior Summaries						
Parameter	N	Mean	Standard Deviation	Percentiles		
				25%	50%	75%
Intercept	10000	-2.2077	0.1555	-2.3142	-2.2062	-2.1004
CDD	10000	0.1063	0.0636	0.0623	0.1065	0.1501
RAIN	10000	-0.4343	0.1911	-0.5599	-0.4309	-0.3036
WW	10000	-0.00453	0.0631	-0.0469	-0.00436	0.0376

Mean is one central value of the posterior (analogous to a point estimate).

Standard deviation is analogous to the standard error in frequentist analysis.

Posterior Intervals					
Parameter	Alpha	Equal-Tail Interval		HPD Interval	
Intercept	0.050	-2.5109	-1.9063	-2.4996	-1.8987
CDD	0.050	-0.0173	0.2277	-0.0172	0.2277
RAIN	0.050	-0.8237	-0.0664	-0.8168	-0.0617
WW	0.050	-0.1278	0.1204	-0.1305	0.1154

Two ways of getting the 95% credible intervals: percentiles and HPD. (HPD may be more accurate).

Posterior Correlation Matrix				
Parameter	Intercept	CDD	RAIN	WW
Intercept	1.000	0.261	-0.512	-0.240
CDD	0.261	1.000	-0.583	-0.796
RAIN	-0.512	-0.583	1.000	0.082
WW	-0.240	-0.796	0.082	1.000

Interpretation is easier when the parameters are not correlated (not required)

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Posterior Autocorrelations				
Parameter	Lag 1	Lag 5	Lag 10	Lag 50
Intercept	0.2759	-0.0108	0.0018	0.0179
CDD	0.2816	-0.0001	-0.0076	0.0007
RAIN	0.3259	0.0161	-0.0101	0.0046
WW	0.2758	-0.0104	0.0052	-0.0093

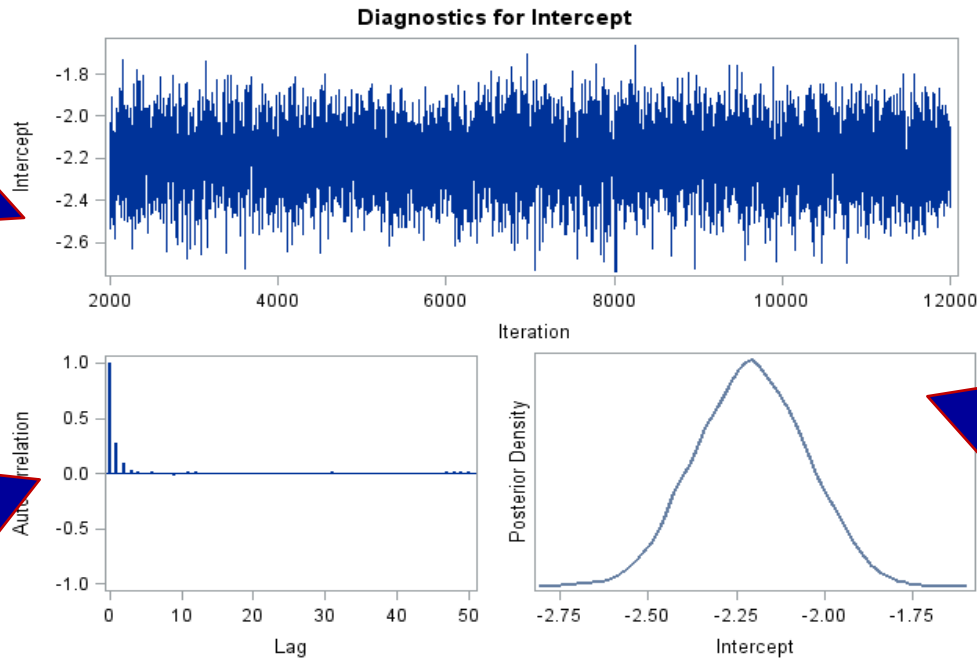
Geweke Diagnostics		
Parameter	z	Pr > z
Intercept	-0.0519	0.9586
CDD	-0.5222	0.6015
RAIN	0.9912	0.3216
WW	-0.4806	0.6308

Effective Sample Sizes			
Parameter	ESS	Autocorrelation Time	Efficiency
Intercept	5557.0	1.7995	0.5557
CDD	5478.8	1.8252	0.5479
RAIN	4660.2	2.1458	0.4660
WW	5523.2	1.8106	0.5523

Some diagnostics:
Autocorrelations at selected lags (nice to see ~ 0).
Geweke statistics should ideally be not significant ($\text{Pr} > 0.05$).

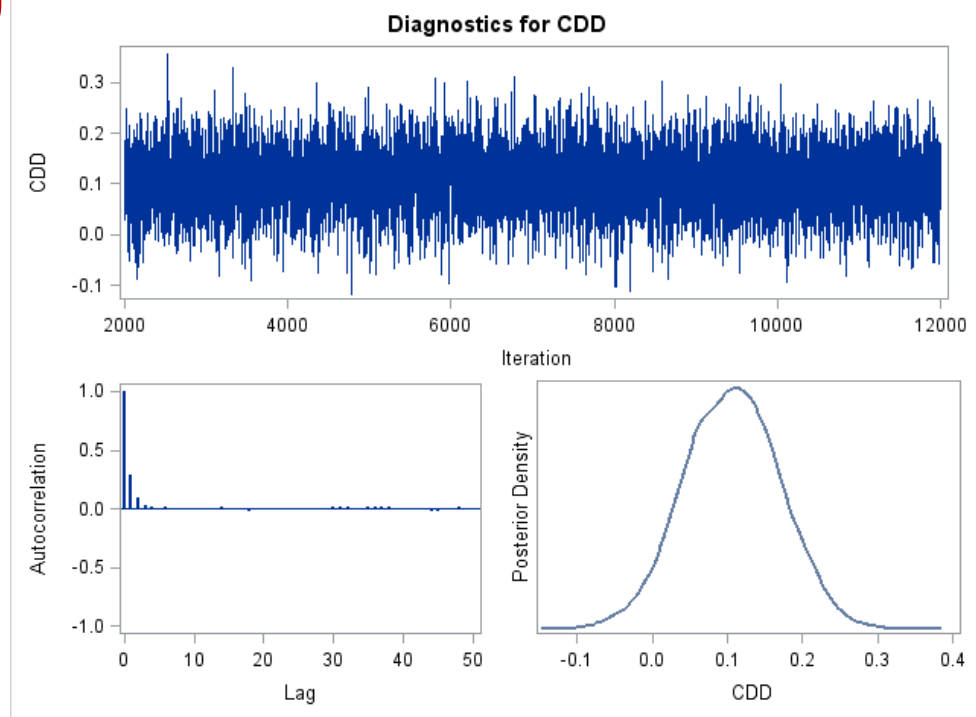
Effective sample sizes should be similar to the selected N for the posterior sampling (a much smaller number means that samples are too highly correlated).

A good trace plot of the N=10000 samples (stable, no trend, frequently crossing the mean line)

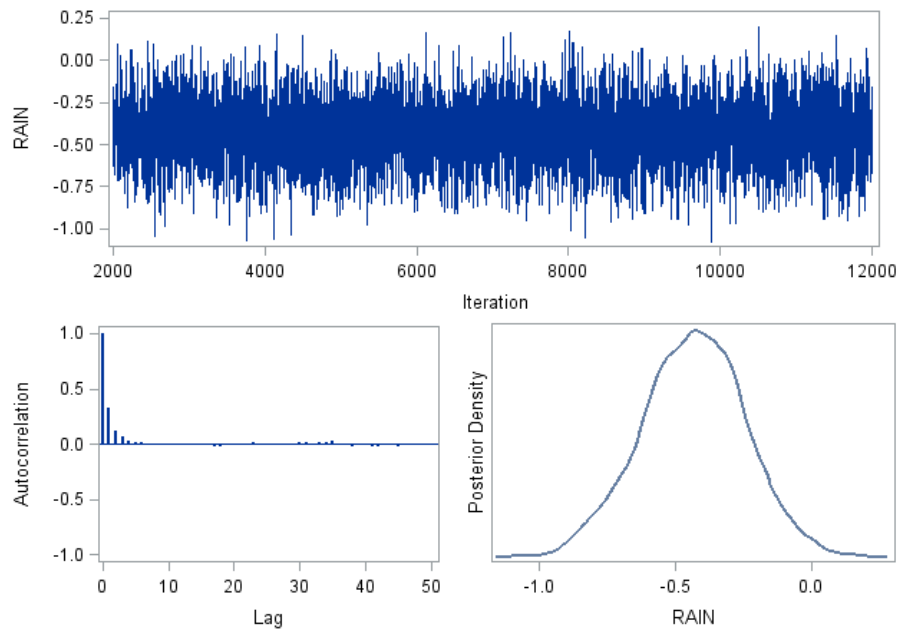


The estimated posterior density function, determined by a so-called kernel smoothing of the N MCMC samples

Ideally, the autocorrelation should drop rapidly towards 0 (indicating independence of the MCMC samples)



Diagnostics for RAIN



Diagnostics for WW

